

# A Continuous-Based Model for the Analysis of Indoor Spaces

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# INTRODUCTION

CONTINUOUS-BASED MODEL FOR INDOOR  
SPACES

# From Large to Small Scale Environments

- People spend large parts of their lives in indoor spaces : office buildings, shopping center, airports...
- Emerging and continuing advances in ambient devices and systems and communications bring novel opportunities for indoor “geo-services”
  - Human way-finding and navigation in built environments
  - Evacuation routes for people stuck in a building during an emergency
  - Tracking suspicious moving objects in a building using video surveillance...
- Is there any need to reconsider current GIS models when considering indoor environments ?
  - Taking into account human cognition and behaviours in such environments
  - The way indoor spaces are constrained by architectural designs
  - Considering the role played by smart location-based devices
  - Taking into account the range of applications in indoor environments...

# Research Issues and Objectives

- **Modelling issues :**
  - How to spatially represent an indoor space ? (discrete, continuous, symbolic)
  - How to transform/map an indoor physical space towards a spatial-based model ?
  - How to take into account the behaviour and positioning data of a moving object and an indoor-based model ?
  - How to apply the model of an indoor space to a given phenomena, either discrete or continuous ?
- **Modelling approach**
  - We retain a continuous and structural-based modelling approach allowing the integration of graph-based properties
  - Such an approach favours accurate indoor positioning, tracking and navigation and the modelling of continuous phenomena
  - The approach is illustrated by the diffusion of a gas leak

# RELATED WORKS

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**MODELLING BACKGROUND**

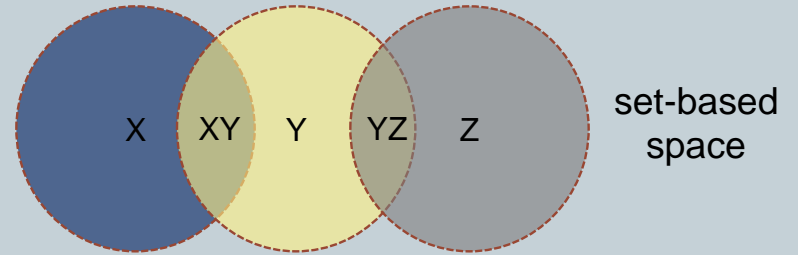
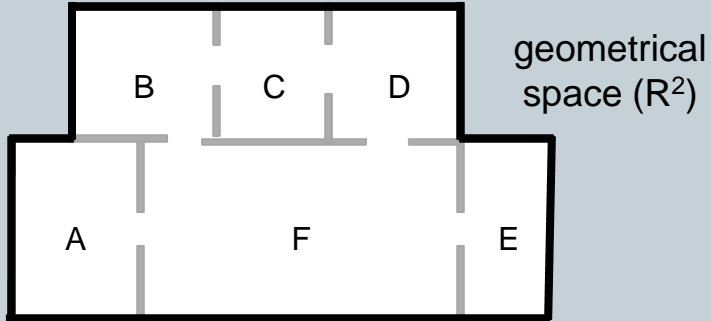
# Modelling Indoor Spaces

- From physical to conceptual modelling : geometric → set-based → topological → semantic
- Geometric spaces :
  - Representation mainly based on Euclidean geometry
  - Using by absolute or relative coordinate systems and transformation between them
- Symbolic spaces (spaces with qualitative description)
  - Set-based representation where space is described by spatial regions and relationships between them
  - Structural representation where topological relationships and structural properties are derived from a graph-based model
  - Semantic representation where space is considered as a set of objects and relationships between them

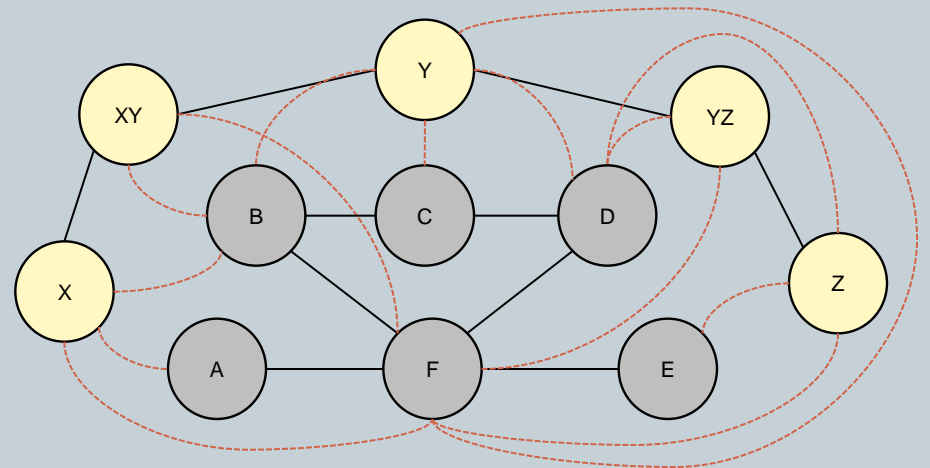
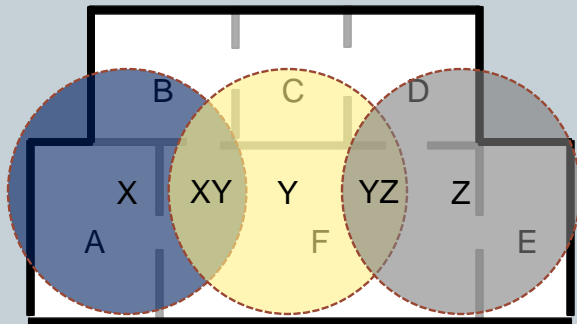
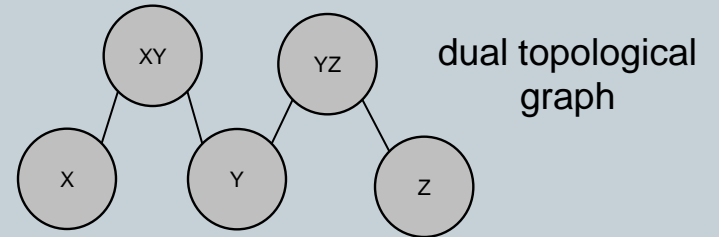
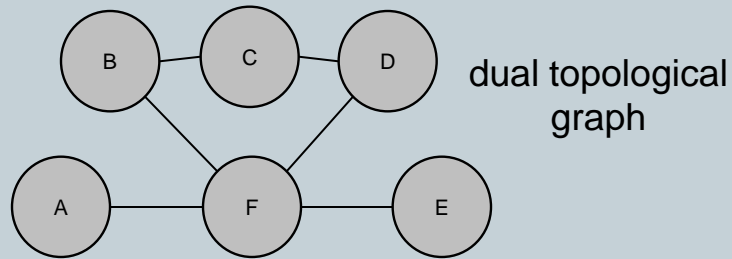
# Modelling Indoor Spaces

Adapted from Li, 2008

Primal spaces



Dual spaces



# Symbolic Spaces vs. Geometric spaces

- Symbolic models of indoor space are often preferred over traditional geometric models because they are able to capture the semantics associated with indoor entities (Jensen *et al.*, 2009)
- Non-exhaustive advantages of symbolic models
  - Simple models generally based on graph models and theory
    - Nodes represent rooms, and edges connections, such as corridors and doors, between rooms
    - Nodes and edges obtained by division, adjacency and connectivity
  - Cells (nodes, edges, objects) define a location reference for indoor space
  - Ambient systems emerge with appropriate positioning systems (presence sensors vs. position sensors)
  - Geometry is approximated as each cell may have (or not) its own geometry
  - Topology is implicit as cell connections reflect the structure of space
  - Spatial relationship between cells and moving object can be established

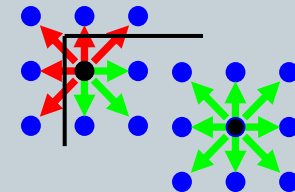


# Is Symbolic Representation Always Appropriate?

- Space syntax had been long applied to indoor environment (e.g. Kim *et al.*, 2008)
  - Well defined from a spatial modelling point of view, and with operators long identified by graph theories
  - Local operators evaluate the connectivity of a given room, while global operators measure the role played by a given room in the whole network
- The assumption of this modelling approach is that there might have a correlation between structural patterns that emerge from layout and the way moving objects (phenomenon) evolve through spaces...
- ..., but
  - There is a lack of continuity and geometrical measures of space or time that encompass another class of properties (such as “continuous” events)
  - People’s behaviours are often non deterministic processes that cannot always be approximated by a structural representation of space

# Towards a Finer Modeling Approach

- Usual node-edge representation is structural and reveals the main spatial structure of a built environment
- While such a model can represent topological relationships, It fails to retain the whole semantics of complicated indoor spaces
  - For example, is a single point enough to represent a room with a large area or an irregular shape?
- Alternative solutions considering indoor spaces at a lower level of granularity should be considered (Ray *et al.*, 2009)
  - A fine “cell-based” modelling approach is based on an occupancy grid that reflects the main geometrical properties
  - Each cell/node is connected to its neighbours that represents connectivity and displacement opportunities



# INDOOR MODELLING

**NODE-EDGE GRAPH WITHIN OCCUPANCY GRID**

# Modelling Background

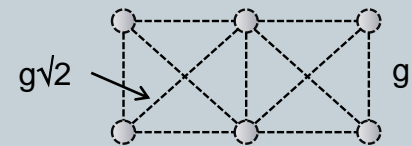
- From an **occupancy grid** as initially introduced in mobile robotics and artificial intelligence
- Where an occupancy grid is a regular matrix consisting of **equally-sized cells**
- In such approach, the surrounding environment of a mobile robot is represented by the occupancy grid
  - Movement opportunities and/or probabilities can be estimated
  - E.g., an high probability of displacement is given to cells relatively connected, while a low probability to cells surrounded by obstacles
- Simplicity and metric embeddedness are two advantages of the occupancy grid approach

# Modelling Principles

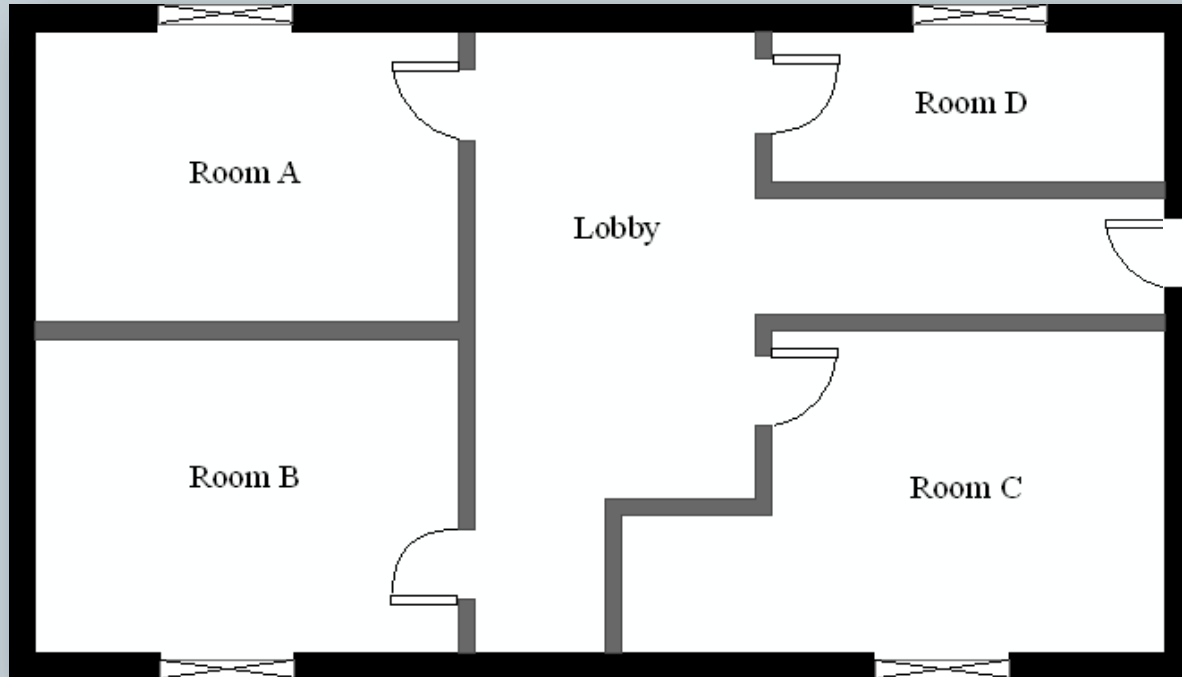
- **Indoor modelling based on :**
  - A node-edge graph that covers all the indoor space
  - Where nodes represent cells within an occupancy grid, and connections between cells are materialized by edges
  - Where impedance values are given to each edge depending of the application of interest
- **Modelling properties**
  - The graph-based model retain displacement opportunities from a continuous point of view
  - Structural properties can be encapsulated within the graph-based representation
  - The geometrical properties are implicitly represented by the continuous layout of the graph and reflect the shapes of the rooms considered

# Modelling Principles

- A built environment is modelled as a **two dimensional space** of extent  $S$  materialized as a continuous space of cellular units
- The continuous representation covering  $S$  is parameterized by a level of **granularity  $g$**  that generates a grid graph of step  $g$
- The grid graph includes additional **diagonal edges** so that each node is connected to 8 neighbours
- Nodes and edges are labelled according to their **memberships to a given cellular unit** such as a room or a connecting space
  - Each node has one and only one membership value as a node is contained by one and only one cellular unit
  - Membership value of an edge is multi-valued when this edge intersects several cellular units



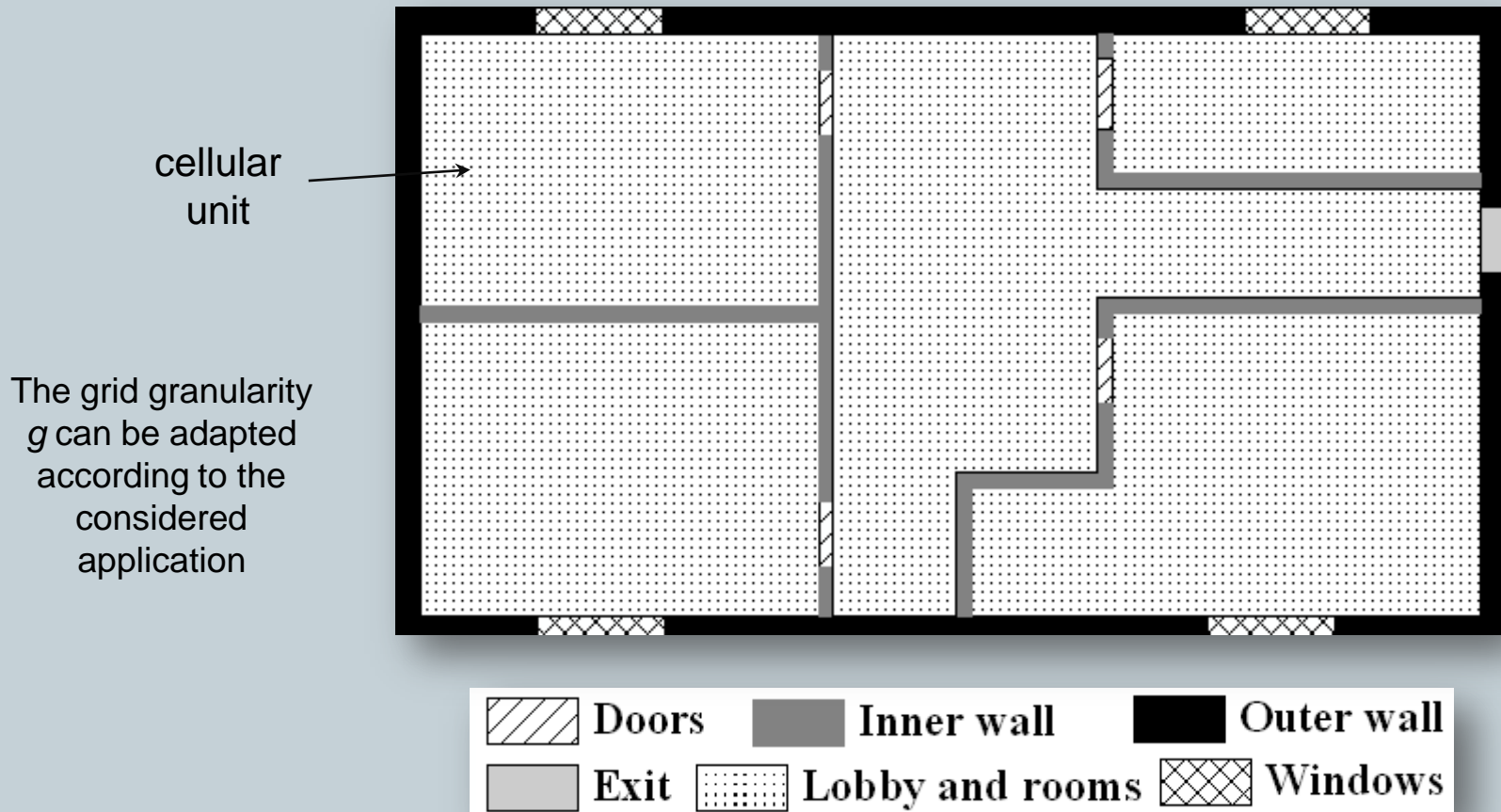
# Modelling Illustration



A floor plan

# Cellular Units

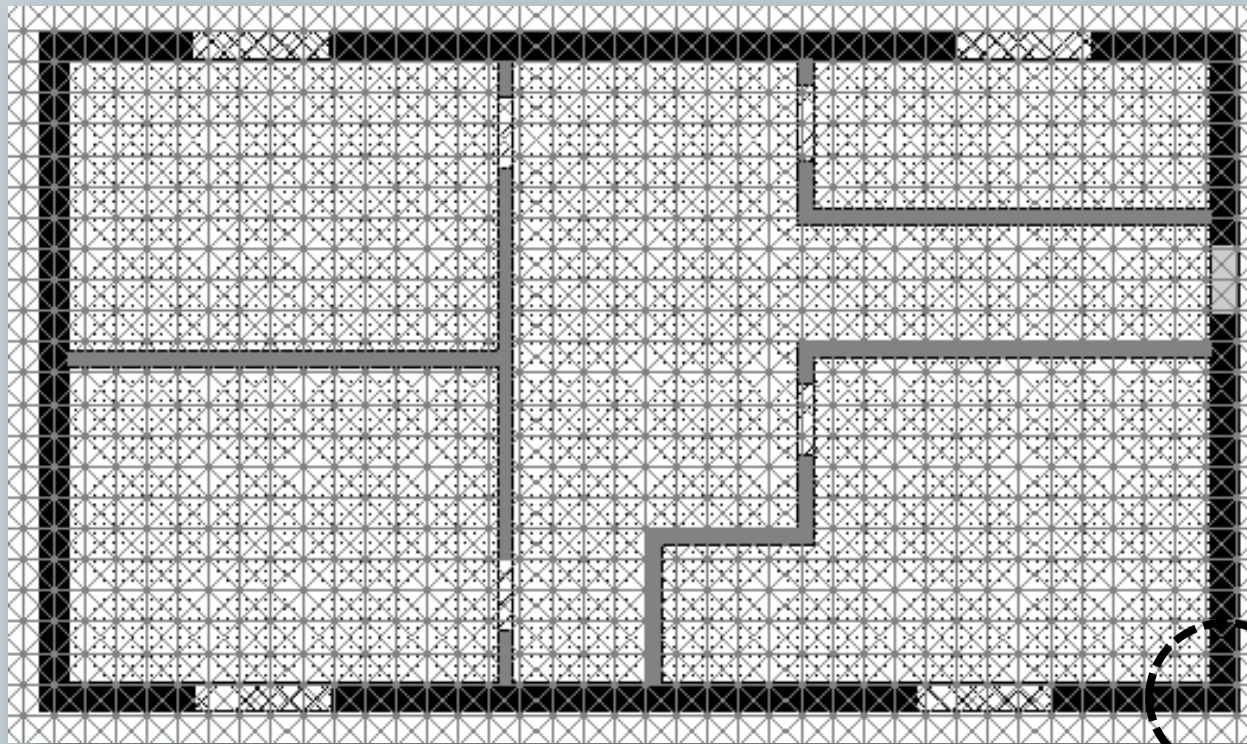
- Each cellular unit contains nodes regularly placed (every  $g$ ). Nodes are labelled according to their memberships to a cellular unit





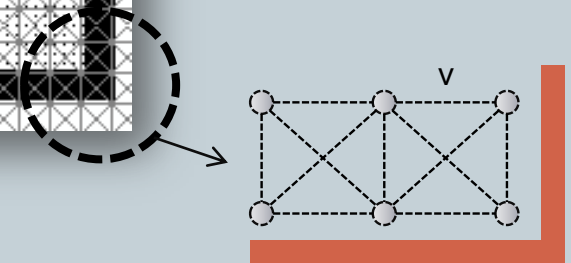
# Grid Graph

- Edge impedance ( $v$ ) allows modelling of different constraints associated to studied phenomena



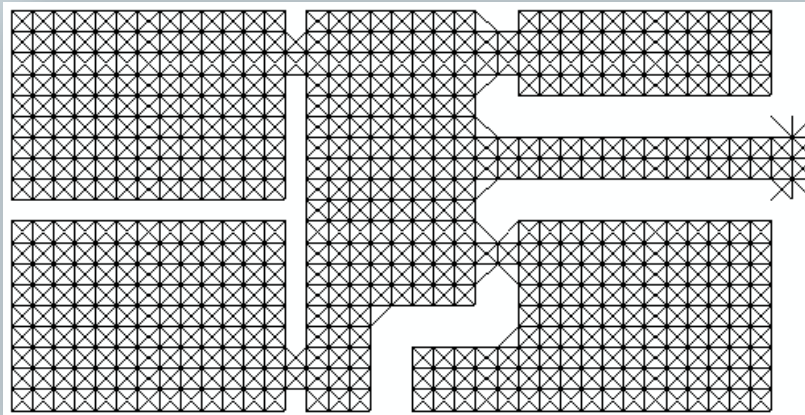
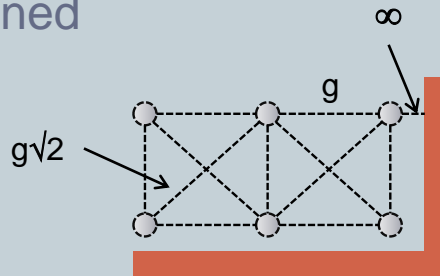
Overlap of a grid graph and labeled cellular units

Impedance values might be correlated with  $g$ . They are closely related to studied application

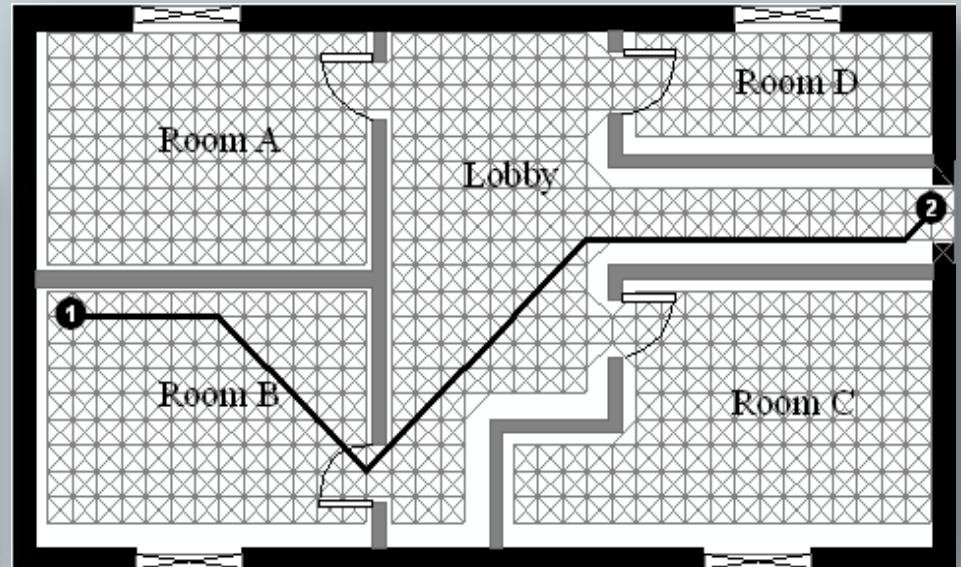


# Illustration for Moving Objects

- The model allows finding accurate shortest path between two points
  - Impedances are based on graph granularity  $g$  and assigned according to cellular unit membership
  - Doors opened



Free space represented by a grid graph



Shortest path between 1 and 2

# CASE STUDY

MAPPING GAS LEAK IN AN INDOOR SPACE

# Objective and Assumptions

- Objective : to map the diffusion of a gas leak in an indoor space
- Some assumptions :
  - The source of the gas leak is located in a given room of an indoor space
  - The impedance of each edge equals the time it takes gas to diffuse along the edge
  - The diffusing speed is denoted as  $s$  in the free space considered, let  $T$  be  $g/s$
- Example of edge impedance values for gas diffusion in an indoor space

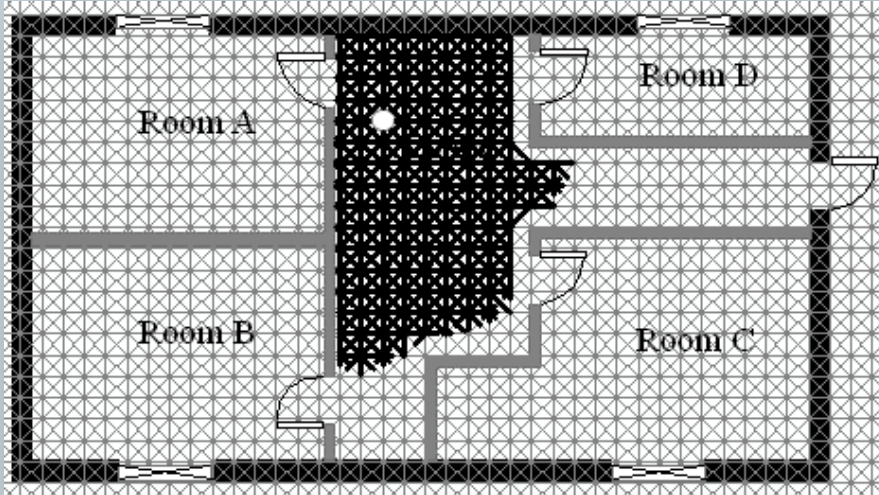
| Description  | Edge length  | Impedance       |
|--|--------------|-----------------|
| Edges are completely within free space: room, lobby, opened door, opened window, or opened exit                      | $g$          | $T$             |
|  | $g.\sqrt{2}$ | $T.\sqrt{2}$    |
| Edges are completely within or intersect less occupied space: closed door, closed window, closed exit, or inner wall | $g$          | $40.T$          |
|  | $g.\sqrt{2}$ | $40.T.\sqrt{2}$ |
| Edges are completely within or intersect more occupied space: outer wall   | $g$          | <i>Infinity</i> |
|  | $g.\sqrt{2}$ | <i>Infinity</i> |

# Algorithm Principles

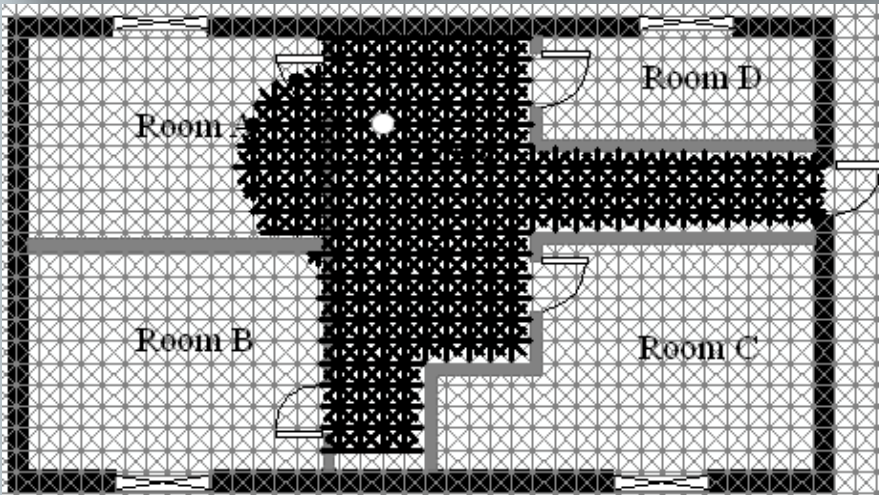
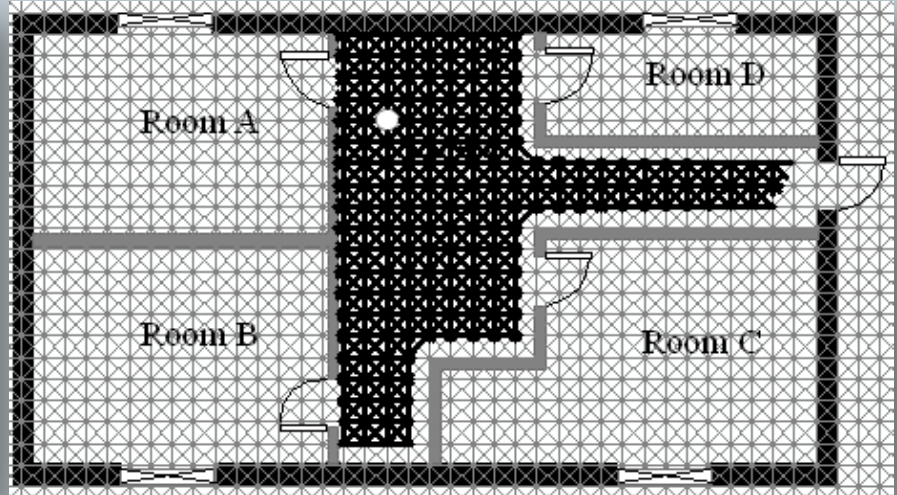
- The diffusion algorithm figures out the evolution of nodes and edges covered by gas diffusion
- Algorithm Principles
  - Let  $n_0$  denote the node representing the source of gas leak, and  $t_0$  the starting time of leak
  - For a given time instant  $t_0+mT$ , where  $m$  is a real number
    - Find all nodes whose shortest paths to  $n_0$  are less than  $mT$  in terms of cost (i.e., diffusing time)
    - Check each edge through examining its two associated nodes and figure out those covered by gas during the interval from  $t_0$  to  $t_0+mT$
    - If not the whole but a part of an edge is covered by the phenomenon, only the covered part is considered

# Mapping Gas Leak in an Indoor Space

$t=t_0+10T$



$t=t_0+20T$



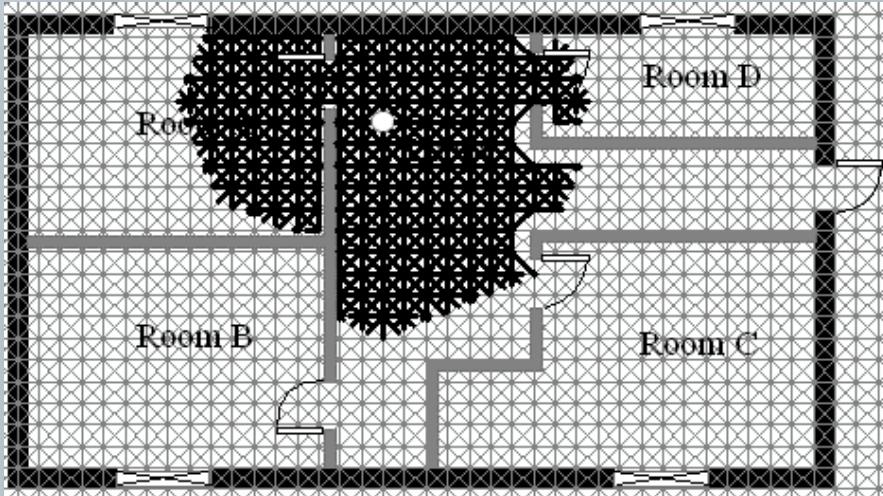
$t=t_0+45T$

Gas leak when all doors are **closed**

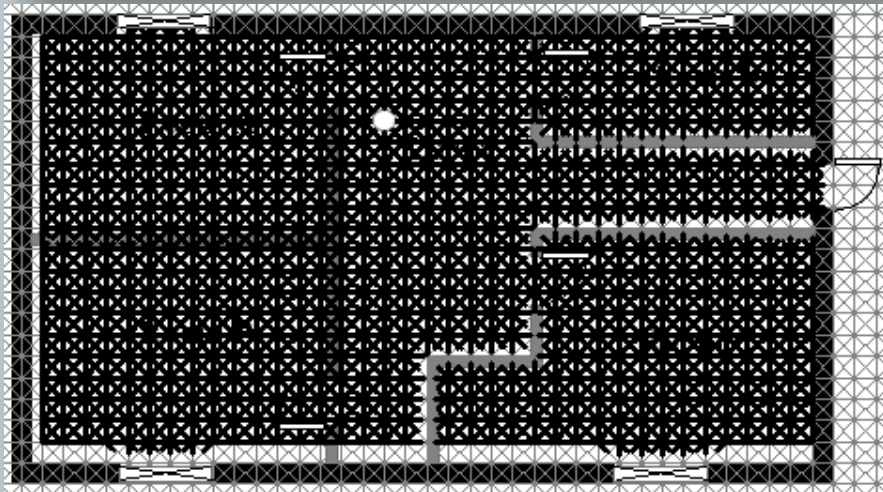
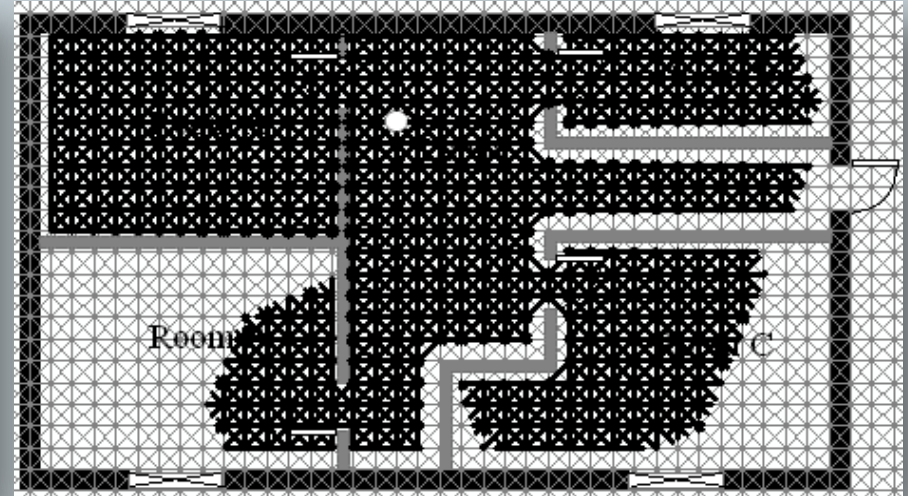
- Starting point of the phenomenon

# Mapping Gas Leak in an Indoor Space

$t=t_0+10T$



$t=t_0+20T$



Gas leak when all doors are **opened**

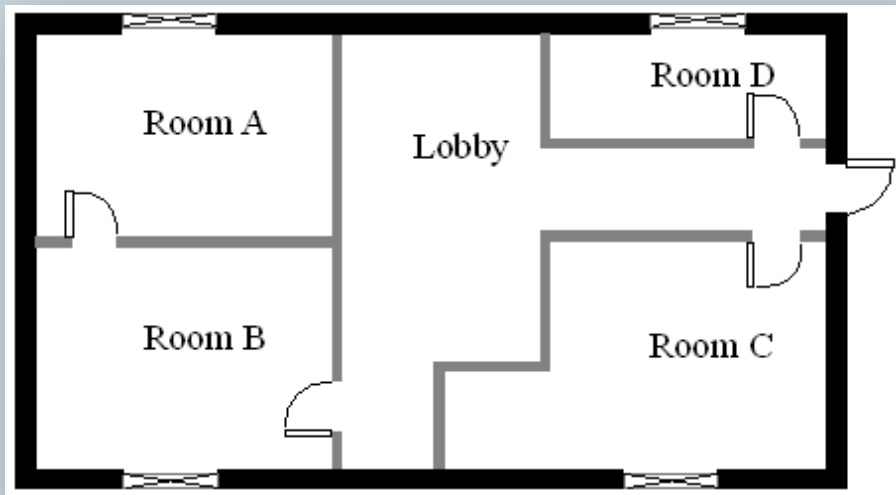
- Starting point of the phenomenon

$t=t_0+45T$

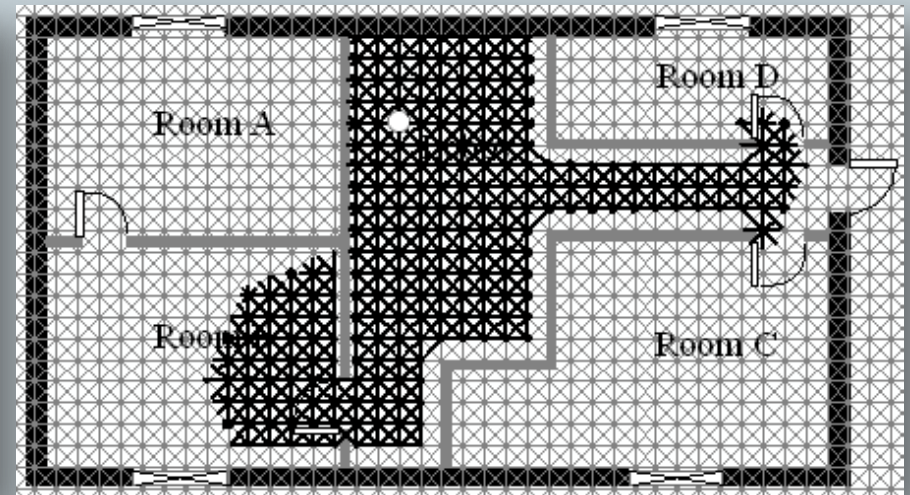
# Mapping Gas Leak in an Indoor Space

- Beyond the evaluation of existing structural configurations face to phenomenon...
- ... another objective can be to identify “best” structural configuration(s)

What if doors' locations are changed ?



Another configuration with all  
**doors opened**



Result at  $t=t_0+20T$



# Centrality Measures

- Similarly to space syntax studies (at structural level), various measures of the centrality (e.g. degree centrality, betweenness, closeness, eigenvector centrality) can be applied to such fine-grain indoor models
- Betweenness is a representative centrality measure applied to graphs (Bonacich, 1987)
  - Denotes the number of time a given node appears in shortest paths between the other nodes of the graph
  - The most central a node is, the most important its centrality role in the structure of the whole graph (i.e., indoor space)

$$C_B(n_a) = \sum_{a \neq j \neq i} \frac{\sigma_{ij}(n_a)}{\sigma_{ij}}$$

betweenness of  
a node  $n_a$

number of the shortest  
paths between nodes  $n_i$   
and  $n_j$  that  $n_a$  lies on

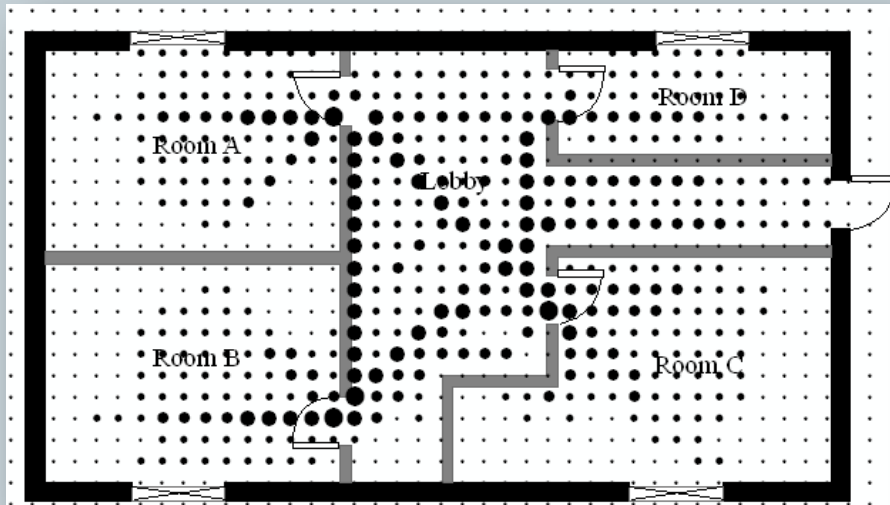
number of the shortest  
paths between nodes  
 $n_i$  and  $n_j$

# Results of Centrality Measures

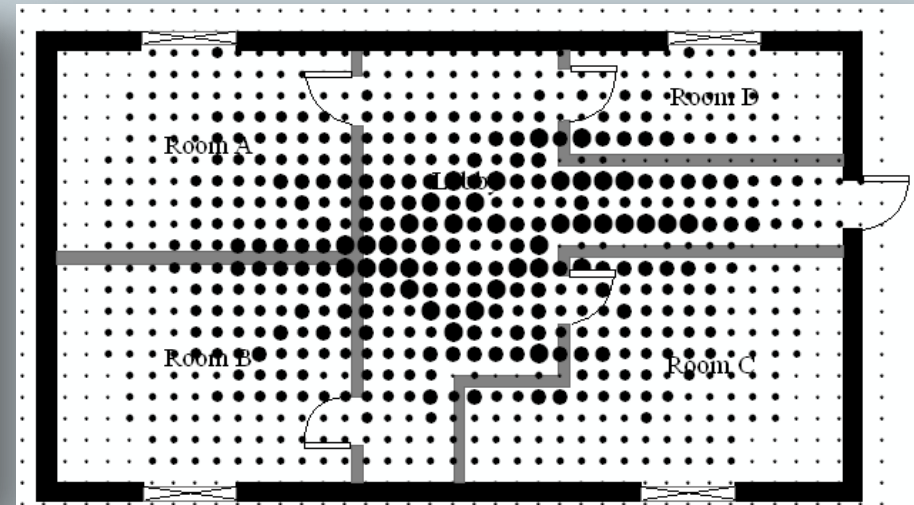
- Betweenness values are classified in five categories (black circles)

nodes with high betweenness values are located in the central area

nodes located in the lobby or around doors play a specific role in the spatial layout



All doors are opened



All doors are closed

- Interest : study the impact of different distribution layouts with respect to a given phenomenon

# CONCLUSION

CONTINUOUS-BASED MODEL FOR INDOOR  
SPACES

# Conclusion

- Built environment and indoor spaces represent a novel domain of GIS applications
- Early developments have been often successful in defining spatial representations of built environments such as structural-based models, cognitive and quantitative models
- The concept of space as considered in indoor environments deserves complementary spatial modelling approaches adapted to the specific continuous properties of built environments

# Conclusion

- The proposed model is a continuous-based representation of a built environment
  - An occupancy grid is considered as the reference modelling concept
  - An interest of this approach is that the coverage of the emerging graph allows
    - A study of the spatial diffusion of a given phenomenon of interest
    - The application of structural measures that reveal some emerging structural properties of the represented space
- The approach thus keeps a continuous representation of space, while still embedding structural properties at a lower level of granularity
- Future efforts will be made to
  - Extend the modelling approach to 3D environments
  - Apply these modelling concepts to real-time positioning, tracking and navigation of pedestrian

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